

## Crystal structure and cationic ordering in ludwigites $\text{Co}_{3-x}\text{Ni}_x\text{BO}_5$

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The structure and composition of two solid solutions of  $\text{Co}_{3-x}\text{Ni}_x\text{BO}_5$  with the ludwigite structure, the nickel ion concentrations in which are  $x = 0.33$  and  $x = 0.59$ , are determined. Within the framework of the first-principles calculation, the cationic ordering for three concentrations  $x = 0.25, 0.5, 0.75$ . It was found that nickel cations prefer to occupy positions 2a and 4g.

**Keywords:** ludwigite, cation ordering, crystal structure.

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### 1. Introduction

Transition metal borates are of interest because they can be realized in various structural types. There are known compounds  $\text{Mn}_3\text{B}_2\text{O}_6$ ,  $\text{Co}_3\text{B}_2\text{O}_6$  with a kotoite structure [1,2],  $\text{Mn}_3\text{BO}_5$ ,  $\text{Co}_3\text{BO}_5$  with ludwigite structure [3,4] and  $\text{Mn}_2\text{BO}_4$  with the structure of warwickite [5], manganese tetraborate  $\text{MnB}_4\text{O}_7$  [6] and others [7]. Depending on the crystallization conditions, one or another structural type of borates can occur, which, in turn, significantly affects the properties of compounds. So, cobalt ions enter only in the divalent state in  $\text{Co}_3\text{B}_2\text{O}_6$  with a kotoite structure, a transition to the antiferromagnetic state is observed in the compound [8]. Cobalt ions are present in trivalent and divalent states in ludwigite  $\text{Co}_3\text{BO}_5$ , with trivalent ions in a low spin state with spin 0, and the magnetic ordering is ferrimagnetic [9].

It is known about the existence of solid solutions of  $\text{Co}_{3-x}\text{Ni}_x\text{BO}_5$  with a kotoite structure [1,6,10–12], however, solid solutions of  $\text{Co}_{3-x}\text{Ni}_x\text{BO}_5$  with ludwigite structure are not currently studied. The spin state of cobalt ions can change from low spin (at high concentrations) to high spin in  $\text{Co}_{3-x}\text{Ni}_x\text{BO}_5$  compounds, depending on the concentration (at concentrations  $x$ , close to 1). In addition, many ludwigites are characterized by the division of the magnetic system into two magnetic subsystems with a non-collinear orientation of the magnetic moments of the subsystems [13–17]. The division into two magnetic subsystems may also occur in solid solutions of  $\text{Co}_{3-x}\text{Ni}_x\text{BO}_5$  if trivalent cobalt ions are in a high spin state. Substitution of cobalt ions with nickel ions in the divalent subsystem and obtaining of crystals  $\text{Co}^{3+}\text{Ni}_{2-x}^{2+}\text{Co}_x^{2+}\text{BO}_5$  with ludwigite structure is an interesting growth problem that was first solved by us in the previous study [12]. Our studies showed that it is necessary to control the valence of cobalt cations for obtaining  $\text{Co}^{3+}\text{Ni}_{2-x}^{2+}\text{Co}_x^{2+}\text{BO}_5$  crystals with a ludwigite structure from melt solutions. A change of the

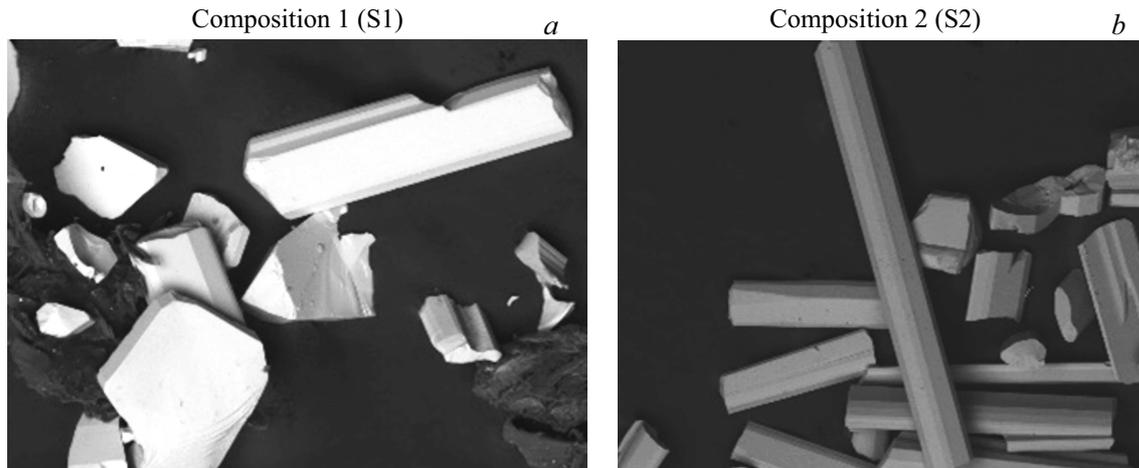
valence of cobalt from 3+ to 2+ results in the growth of borates with a graphite structure in which metal ions are present only in the divalent state. It was shown in Ref. [12] that compounds crystallized into a phase with a ludwigite structure at low concentrations of nickel ions in the solution-melt system; the crystallization phase was a phase with a kotoite structure with an increase of the concentration of nickel ions. We present in this paper a study of the compositions, crystal structure and cationic ordering of compounds  $\text{Co}^{3+}\text{Ni}_{2-x}^{2+}\text{Co}_x^{2+}\text{BO}_5$  with the ludwigite structure obtained in the study [12].

### 2. Composition and crystal structure

Two compositions  $\text{Co}^{3+}\text{Ni}_{2-x}^{2+}\text{Co}_x^{2+}\text{BO}_5$  with ludwigite structure were obtained by spontaneous generation from a solution-melt system based on  $\text{Bi}_2\text{Mo}_3\text{O}_{12}-\text{B}_2\text{O}_3$ , diluted with alkali metal carbonates  $\text{Na}_2\text{CO}_3$  [12]. The synthesized crystals are have a black color with a needle-like shape (Figure 1). The obtained single crystals were studied using the TM-4000Plus tabletop scanning electron microscope by Hitachi at an accelerating voltage of 20 kV. Element mapping was carried out using Bruker XFlash 630Hc X-ray detector. Spectra were analyzed using Quantax70 software. All samples had uniform compositions. The spectra of different crystal sites for all groups of samples were compared to check the uniformity.

Images of crystals are shown in Figure 1. The ratios of nickel and cobalt ions, determined using the scanning microscopy method, and the chemical formulas of the compounds for the two compositions are given in Table 1, the ratios of transition metal ions in the melt-solution are also indicated there.

It can be seen from the table that there is a qualitative agreement between the content of ions in the „flux“ and the actual content of nickel and cobalt in the compounds.



**Figure 1.** Photos of samples of solid solutions of  $\text{Co}_{3-x}\text{Ni}_x\text{BO}_5$  obtained using a desktop scanning electron microscope: a) composition S1, b) composition S2.

**Table 1.** Comparison of the actual composition of the obtained samples and the composition of „flux“ for each sample

Composition	Ratio of Ni:Co		Chemical formula
	in solution-melt	in crystal	
S1	1:11	1:8,1	$\text{Co}^{3+}\text{Ni}_{0.33}^{2+}\text{Co}_{1.67}^{2+}\text{BO}_5$
S2	1:11	1:4,1	$\text{Co}^{3+}\text{Ni}_{0.59}^{2+}\text{Co}_{1.41}^{2+}\text{BO}_5$

However, the actual nickel content exceeds the nickel content in the melt solution, which emphasizes the difference in the distribution coefficients of cobalt and nickel oxides in the used melt solutions — the lower solubility of nickel oxide results in a greater presence of this element in the crystal [12].

### 3. Crystal structure and cationic ordering

The crystal structure was studied on single crystal samples by X-ray diffraction using SMART APEXII diffractometer ( $\text{MoK}\alpha$ ,  $\lambda = 0.7106 \text{ \AA}$ ). The space group, the parameters of the crystal lattice for compositions S1 and S2 are listed in Table 2, and coordinates of atoms for composition S1 are listed in Table 3.

The coordinates of the atoms for the composition of S2 were not specified, since the change in the parameters of the crystal lattice relative to the composition of S1 is less than one percent, it is unlikely that there will be a significant change in the coordinates of the atoms in the crystal lattice. The distances between ions for the composition S1 are provided in Table A1 of the Appendix, the distances  $\text{Me}-\text{O}$  are also indicated below for clarity when comparing different compositions with the ludwigite structure. The metallic ions Co and Ni are indicated in the table as  $\text{Me}$ , since it is impossible to distinguish nickel and

cobalt ions using the X-ray diffraction method, therefore, it is impossible to determine the population of crystallographic positions.

As we noted earlier, metal ions in compositions with the ludwigite structure  $(\text{Me}, \text{Me}')_3\text{BO}_5$  should have different valence according to the condition of electroneutrality. In

**Table 2.** Parameters of the crystal lattice of compositions S1 and S2. Space group  $Pbam$  in both cases (55)

Composition	S1	S2	
$V, \text{ \AA}^3$	332.96(4)	333.76(5)	
$R$ -factor	0.032	0.036	
Parameters of cells, $\text{ \AA}$	$a$	9.2855(7)	9.244(5)
	$b$	11.9893(9)	12.049(5)
	$c$	2.9908(2)	2.9966(14)

**Table 3.** Atomic coordinates  $\text{Co}^{3+}\text{Ni}_{0.33}^{2+}\text{Co}_{1.67}^{2+}\text{BO}_5$  (composition 1).  $U_{\text{iso}}^*$  — isotropic,  $U_{\text{eq}}$  — equivalent isotropic displacement parameters

Atom	Position	Coordinates of atoms			$U_{\text{iso}}^*/U_{\text{eq}}$
		$x/a$	$y/b$	$z/c$	
$\text{Me}_1$	2a	1/2	1/2	0	0.00631(12)
$\text{Me}_2$	2d	0	1/2	1/2	0.00589(12)
$\text{Me}_3$	4g	0.49645(3)	0.77727(3)	0	0.00627(10)
$\text{O}_1$	4g	0.8797(2)	0.57741(17)	0	0.0123(3)
$\text{O}_2$	4h	0.83880(18)	0.76125(16)	1/2	0.0083(3)
$\text{O}_3$	4h	0.65673(19)	0.45974(15)	1/2	0.0087(3)
$\text{O}_4$	4g	0.6133(2)	0.64255(14)	0	0.0091(3)
$\text{O}_5$	4h	0.8821(2)	0.36128(14)	1/2	0.0083(3)
B	4h	0.7346(3)	0.3618(2)	1/2	0.0065(4)

**Table 4.** Calculated differences of energies  $\Delta E$  of various cationically ordered configurations with respect to the lowest energy configuration for the composition  $\text{Co}^{3+}\text{Ni}_{0.25}^{2+}\text{Co}_{1.75}^{2+}\text{BO}_5$ 

Ion №	№ of cationically ordered state												$\Delta E$
	2a		2d		4g				4h				
	1	2	3	4	5	6	7	8	9	10	11	12	
1	Ni	Co	0.031396										
2	Co	Ni	Co	0.028042									
3	Co	Co	Co	Co	Ni	Co	0						
4	Co	Co	Co	Co	Co	Co	Co	Co	Ni	Co	Co	Co	0.026700

**Table 5.** Calculated energy differences  $\Delta E$  of various cationically ordered configurations with respect to the lowest energy configuration for the composition  $\text{Co}^{3+}\text{Ni}_{0.5}^{2+}\text{Co}_{1.5}^{2+}\text{BO}_5$ 

Ion №	№ of cationically ordered state												$\Delta E$
	2a		2d		4g				4h				
	1	2	3	4	5	6	7	8	9	10	11	12	
1	Ni	Ni	Co	0.021299									
2	Co	Co	Ni	Ni	Co	0.017804							
3	Co	Co	Co	Co	Ni	Ni	Co	Co	Co	Co	Co	Co	0.078141
4	Co	Co	Co	Co	Co	Co	Co	Co	Ni	Ni	Co	Co	0.021322
5	Co	Ni	Ni	Co	0.0174404								
6	Ni	Co	Co	Co	Ni	Co	0						
7	Co	Ni	Co	Co	Co	Co	Co	Co	Ni	Co	Co	Co	0.017698
8	Co	Ni	Co	Co	Ni	Co	0.01675						

**Table 6.** Calculated energy differences of various cationically ordered configurations with respect to the lowest energy configuration for the composition  $\text{Co}^{3+}\text{Ni}_{0.75}^{2+}\text{Co}_{1.25}^{2+}\text{BO}_5$ 

Ion №	№ of cationically ordered state												$\Delta E$
	2a		2d		4g				4h				
	1	2	3	4	5	6	7	8	9	10	11	12	
1	Ni	Ni	Co	Co	Ni	Co	0						
2	Ni	Co	Co	Co	Ni	Ni	Co	Co	Co	Co	Co	Co	0.037859
3	Co	Ni	Co	Co	Ni	Ni	Co	Co	Co	Co	Co	Co	0.036366
4	Co	Ni	Co	Co	Co	Co	Ni	Ni	Co	Co	Co	Co	0.000383
5	Co	Ni	Co	Co	Co	Ni	Ni	Co	Co	Co	Co	Co	0.032364
6	Ni	Co	Co	Co	Co	Ni	Ni	Co	Co	Co	Co	Co	0.032362
7	Co	Ni	Co	Co	Ni	Co	Co	Ni	Co	Co	Co	Co	0.032373

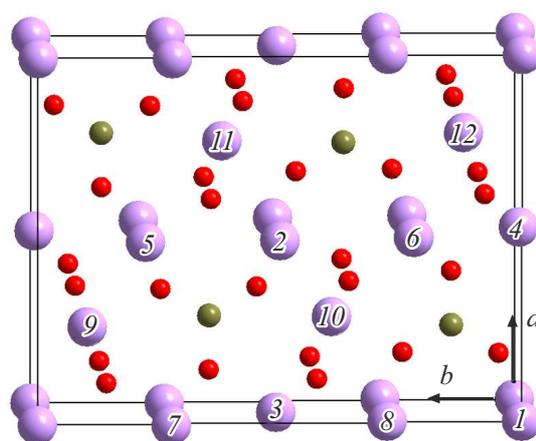
**Table 7.** Distances  $d_{Me-O}$  for each crystallographic position for compounds  $\text{Ni}_2\text{GaBO}_5$  [24],  $\text{Ni}_2\text{AlBO}_5$  [24],  $\text{Co}_3\text{BO}_5$  [3] and  $\text{Co}^{3+}\text{Ni}_{0.33}^{2+}\text{Co}_{1.67}^{2+}\text{BO}_5$  and the ionic radius of the trivalent ion  $r_{Me^{3+}}$ . Indicated for all bonds

Composition	Crystallographic Position	2a	2d	4g	4h	$r_{Me^{3+}}$ , nm
$\text{Ni}_2\text{GaBO}_5$	$d_{Me-O}$ , AA/number of bonds	2.004/2 2.094/4	2.038/2 2.061/4	1.948 2.015 2.102/2 2.105/2	2.052 2.065 1.942/2 2.067/2	0.063 ( $\text{Ga}^{3+}$ )
	$\langle d_{Me-O} \rangle$ , Å	2.064	2.053	2.062	2.022	
	Occupancy, % for $\text{Ni}^{2+}$	100.0	100.0	100.0	0	
$\text{Ni}_2\text{AlBO}_5$	$d_{Me-O}$ , AA/number of bonds	1.972/2 2.070/4	1.97/2 2.012/4	1.96 2.054 2.093/2 2.103/2	1.99 2.01 1.89/2 2.045/2	0.052 ( $\text{Al}^{3+}$ )
	$\langle d_{Me-O} \rangle$ , Å	2.037	1.998	2.067	1.978	
	Occupancy, % for $\text{Ni}^{2+}$	65.2	89.0	85.2	35.8	
$\text{Co}_3\text{BO}_5$	$d_{Me-O}$ , AA/number of bonds	1.998/2 2.142/4	1.988/2 2.101/4	1.944 2.047 2.113/2 2.135/2	1.97 1.98 1.920/2 1.978/2	0.055 ( $\text{Co}^{3+}$ , in low spin state)
	$\langle d_{Me-O} \rangle$ , Å	2.094	2.063	2.081	1.957	
	Occupancy, % for $\text{Co}^{2+}$	100.0	100.0	100.0	0.0	
$\text{Co}^{3+}\text{Ni}_{0.33}^{2+}\text{Co}_{1.67}^{2+}\text{BO}_5$	$d_{Me-O}$ , AA/number of bonds	2.007/2 2.141/4	1.991/2 2.084/4	1.946 2.052 2.126/2 2.143/2	1.993 2.000 1.943/2 2.017/2	? ( not known confidently)
	$\langle d_{Me-O} \rangle$ , Å	2.096	2.053	2.089	1.985	
	Estimated occupancy, % for $Me^{2+}$	100.0	100.0	100.0	0.0	

our case, cobalt ions are trivalent ions in compounds  $\text{Co}_{3-x}\text{Ni}_x\text{BO}_5$ , nickel ions are part of ludwigites in the divalent state. To correctly describe the magnetic properties, it is necessary to know the distribution of magnetic ions in crystallographic positions. The neutron diffraction method is a direct experimental method which can determine the distribution of ions over positions. In addition to the fact that this method is not widely available, it is very difficult to study of borates using the neutron diffraction method because of the high absorption capacity of boron ions. *ab initio* calculations can be used to model the distribution of metal ions over positions. The energies of various cationically ordered configurations can be compared using *ab initio* approaches, determining which distribution of cations by positions is the most advantageous.

The ludwigite unit cell contains 12 transition metal ions, which occupy four crystallographic positions: 2a, 2d, 4g and 4h. The ludwigite structure is shown in Figure 2.

Using the Wien2K software package, we calculated the total energies of various cationically ordered configurations for three compositions:  $\text{Co}^{3+}\text{Ni}_{0.25}^{2+}\text{Co}_{1.75}^{2+}\text{BO}_5$ ,

**Figure 2.** Ludwigite structure. Transition metal ions are indicated by the largest circles and numbered with numbers from 1 to 12. The ions 1 and 2 occupy the position 2a, the ions 3 and 4 occupy the position 2d, ions 5–8 occupy the position 4g, and ions 9–12 occupy the position 4h.

$\text{Co}^{3+}\text{Ni}_{0.5}^{2+}\text{Co}_{1.5}^{2+}\text{BO}_5$ ,  $\text{Co}^{3+}\text{Ni}_{0.75}^{2+}\text{Co}_{1.25}^{2+}\text{BO}_5$ . One cobalt ion is replaced by a nickel ion in the first composition, two cobalt ions are replaced by nickel ions in the second composition, and three cobalt ions are replaced by nickel ions in the third composition.

The Wien2K software package uses the method of linearized coupled plane waves with local orbitals [18,19]. The exchange-correlation energy is calculated in the least squares approximation (LSDA) [20] taking into account the density gradient [21], the Hubbard correlation coefficients are also taken into account. We used the potentials  $U = 0.52$  Ry and  $J = 0$  Ry [22] for transition metal ions in the calculation. A set of 400  $k$  points in the Brillouin zone was used for finding the total energy. Value  $R_{\text{MT}}K_{\text{max}} = 6.0$  ( $R_{\text{MT}}$  — minimum radius of MT spheres,  $K_{\text{max}}$  — plane wave cutoff vector). The accuracy of the energy calculation was  $1 \mu\text{Ry}$ . The following radii of atomic spheres were used in the calculations: 1.91 atomic units for nickel ions, 1.86 at.u. for cobalt ions, 1.13 at.u. for boron ions and 1.31 at.u. for oxygen. The modified Blehl tetrahedron method was used to calculate the total density of states [23].

Tables 4–6 shows the calculated energy differences of various cationically ordered configurations with respect to the configuration with the lowest energy.

Nickel ions primarily replace cobalt ions in positions 4g and 2a as can be seen from Tables 4–6. According to the data obtained by neutron diffraction in ludwigite  $\text{Co}_3\text{BO}_5$ , positions 2a, 2d, 4g are occupied by divalent cobalt ions, and position 4h are occupied by trivalent cobalt ions in the low spin state [9]. The ionic radii of divalent cobalt and nickel ions are close to  $r_{\text{Co}^{2+}} = 0.074$  nm and  $r_{\text{Ni}^{2+}} = 0.072$  nm. Whereas the ionic radii of trivalent cobalt ions are significantly smaller: in the high-spin state  $r_{\text{Co}^{3+}} = 0.061$  nm, and in the low-spin state  $r_{\text{Co}^{3+}} = 0.055$  nm.

The distances  $Me-O$ , as well as the populations of divalent cations for each crystallographic position for four compounds  $\text{Ni}_2\text{GaBO}_5$ ,  $\text{Ni}_2\text{AlBO}_5$ ,  $\text{Co}_3\text{BO}_5$  and  $\text{Co}^{3+}\text{Ni}_{0.33}^{2+}\text{Co}_{1.67}^{2+}\text{BO}_5$  are listed in Table 7 [3,24].

The positions 2a, 2d, 4g are occupied only by divalent nickel and cobalt ions, respectively, in compounds  $\text{Ni}_2\text{GaBO}_5$  and  $\text{Co}_3\text{BO}_5$ . It can be seen in Table 7 that the average distances  $Me-O$  for positions 2a, 2d, 4g in these bonds differ by less than 1.5%, whereas for position 4h the difference is 3.5%. The ionic radius of gallium is greater than the ionic radius of trivalent cobalt in the low spin state, the average bond length is  $\text{Ga}-O$  more than  $\text{Co}-O$ . The trivalent ion has the smallest ionic radius in the  $\text{Ni}_2\text{AlBO}_5$  compound, the trivalent ion is present in this compound with different concentrations in all crystallographic positions, it can be seen that the average length of bond  $Me-O$  for position 2d is less than for other compositions in Table 7. Substitution of cobalt ions for nickel ions in the compound  $\text{Co}^{3+}\text{Ni}_{0.33}^{2+}\text{Co}_{1.67}^{2+}\text{BO}_5$  changes the lengths of bonds  $Me-O$  within 1–2% with respect to  $\text{Co}_3\text{BO}_5$ , the average length of bond  $Me-O$  varies within the same limits, in particular, for

position 4h, which allows assuming that nickel ions replace cobalt ions in the divalent state in positions 2a, 2d, 4g.

## 4. Conclusion

The composition of the two subject solid solutions:  $\text{Co}^{3+}\text{Ni}_{0.33}^{2+}\text{Co}_{1.67}^{2+}\text{BO}_5$  and  $\text{Co}^{3+}\text{Ni}_{0.59}^{2+}\text{Co}_{1.41}^{2+}\text{BO}_5$  was studied using scanning microscopy, the crystal structure, lattice parameters and atomic coordinates were determined. *ab initio* calculation of energies of various cationically ordered configurations showed that nickel ions prefer to replace cobalt ions at positions 2a and 4g, which is qualitatively consistent with experimental data.

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## Conflict of interest

The authors declare that they have no conflict of interest.

## Appendix

Symmetry Codes:

- (i)  $x, y, z-1$ ; (ii)  $x+1, y, z$ ;
- (iii)  $x, y, z+1$ ; (iv)  $-x+1, -y+1, -z$ ;
- (v)  $x-1, y, z$ ; (vi)  $-x+1, -y+1, -z+1$ ;
- (vii)  $x-1, y, z-1$ ; (viii)  $x-1/2, -y+3/2, z$ ;
- (ix)  $-x+3/2, y+1/2, -z+1$ ;
- (x)  $-x+3/2, y+1/2, -z$ ;
- (xi)  $x-1/2, -y+3/2, z+1$ ; (xii)  $x+1/2, -y+3/2, z$ ;
- (xiii)  $x+1, y, z+1$ ; (xiv)  $x+1/2, -y+3/2, z-1$ ;
- (xv)  $-x+3/2, y-1/2, -z+1$ ;
- (xvi)  $-x+3/2, y-1/2, -z$ .

**Table A1.** Distances between atoms in compound  $\text{Co}^{3+}\text{Ni}_{0.33}^{2+}\text{Co}_{1.67}^{2+}\text{BO}_5$ 

$d(\text{Me}-\text{O}), \text{Å}$		$d(\text{Me}-\text{Me}), \text{Å}$		$d(\text{B}-\text{O}), \text{Å}$	
$\text{Co}_1-\text{O}_4$	2.0067(17)	$\text{Co}_1-\text{Co}_1^{\text{i}}$	2.9908(2)	$\text{B}-\text{O}_3$	1.379(3)
$\text{Co}_1-\text{O}_4^{\text{vi}}$	2.0068(17)	$\text{Co}_1-\text{Co}_1^{\text{iii}}$	2.9908(2)	$\text{B}-\text{O}_5$	1.370(3)
$\text{Co}_1-\text{O}_3$	2.1418(13)			$\text{B}-\text{O}_2^{\text{xvi}}$	1.385(3)
$\text{Co}_1-\text{O}_3^{\text{iv}}$	2.1418(13)				
$\text{Co}_1-\text{O}_3^{\text{iii}}$	2.1418(13)				
$\text{Co}_1-\text{O}_3^{\text{vi}}$	2.1418(13)				
$\text{Co}_2-\text{O}_5^{\text{iv}}$	1.9910(17)	$\text{Co}_2-\text{Co}_4^{\text{v}}$	2.7566(3)	–	–
$\text{Co}_2-\text{O}_5^{\text{vi}}$	1.9910(17)	$\text{Co}_2-\text{Co}_4^{\text{iv}}$	2.7566(3)		
$\text{Co}_2-\text{O}_1^{\text{vi}}$	2.0847(13)	$\text{Co}_2-\text{Co}_2^{\text{ii}}$	2.9908(2)		
$\text{Co}_2-\text{O}_1^{\text{iii}}$	2.0847(13)	$\text{Co}_2-\text{Co}_2^{\text{i}}$	2.9908(2)		
$\text{Co}_2-\text{O}_2^{\text{iv}}$	2.0847(13)				
$\text{Co}_2-\text{O}_1^{\text{v}}$	2.0847(13)				
$\text{Co}_3-\text{O}_4$	1.9456(18)	$\text{Co}_3-\text{Co}_3^{\text{iii}}$	2.9908(2)	–	–
$\text{Co}_3-\text{O}_1^{\text{viii}}$	2.052(2)	$\text{Co}_3-\text{Co}_3^{\text{i}}$	2.9908(2)		
$\text{Co}_3-\text{O}_5^{\text{ix}}$	2.1265(13)				
$\text{Co}_3-\text{O}_5^{\text{x}}$	2.1265(13)				
$\text{Co}_3-\text{O}_2^{\text{viii}}$	2.1430(12)				
$\text{Co}_3-\text{O}_2^{\text{xi}}$	2.1430(12)				
$\text{Co}_4-\text{O}_4^{\text{i}}$	1.9431(12)	$\text{Co}_4-\text{Co}_2^{\text{ii}}$	2.7566(3)	–	–
$\text{Co}_4-\text{O}_4$	1.9431(12)	$\text{Co}_4-\text{Co}_4^{\text{i}}$	2.9908(2)		
$\text{Co}_4-\text{O}_3$	1.9930(19)	$\text{Co}_4-\text{Co}_4^{\text{iii}}$	2.9908(2)		
$\text{Co}_4-\text{O}_2$	1.9998(19)				
$\text{Co}_4-\text{O}_1$	2.0170(13)				
$\text{Co}_4-\text{O}_1^{\text{i}}$	2.0170(13)				

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